



**PHILADELPHIA UNIVERSITY
DEPARTMENT OF BASIC SCIENCES**

Final Exam A

DISCRETE STRUCTURES

14–6–2007

PART (I) Each problem is worth 3 points. Circle one answer.

1) Convert the proposition $p \rightarrow (q \oplus q)$ to CNF.

- a) $(\neg p \vee \neg q) \wedge (p \vee q)$ b) $(\neg p \vee q) \wedge (p \vee \neg q)$
c) $(\neg p \vee \neg q) \wedge (\neg p \vee q)$ d) $(\neg p \vee q) \wedge (p \vee q)$

2) The number 5234 is in octal. Convert it to hexadecimal.

- a) A8E b) B9E c) B8C d) A9C

3) The sequence 3,7,6,10,11,15,... is given by the following recursive relation.

- a) $f(n) = \left\lfloor \frac{f(n-1) + f(n-2)}{2} \right\rfloor$ b) $f(n) = \left\lfloor \frac{f(n-1)}{2} \right\rfloor + f(n-2)$
c) $f(n) = f(n-1) + \left\lfloor \frac{f(n-2)}{2} \right\rfloor$ d) $f(n) = \left\lfloor \frac{f(n-1)}{2} \right\rfloor + \left\lfloor \frac{f(n-2)}{2} \right\rfloor$

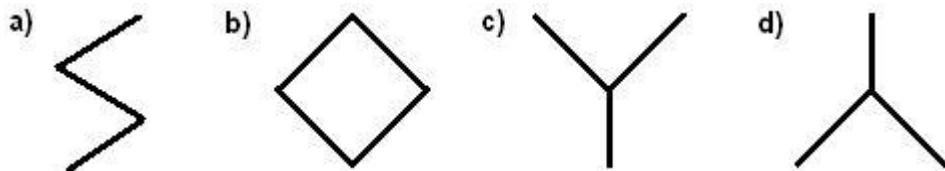
4) One of these sets is equal to $A - B$.

- a) $(A \oplus B) \cap A$ b) $(A \oplus B) \cap B$ c) $(A - B) \oplus A$ d) $(A - B) \oplus B$

5) Find the number of integer solutions to $x + y + z = 50$ satisfying the conditions $x \geq 5$ and $y \geq 8$ and $z \geq 10$.

- a) 406 b) 351 c) 300 d) 253

6) $A = \{4, 8, 12, 24\}$ and $R = \{(a, b) \mid a \text{ divides } b\} \subseteq A \times A$. The Hasse diagram is



7) How many permutations from the letters {A, C, E, M, N, S, T} contain the word AN or SET ?

- a) 738 b) 234 c) 816 d) 142

8) Which graph has no Euler path/circuit and no Hamilton path/circuit?

a) K_{2,5}

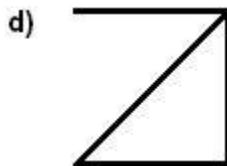
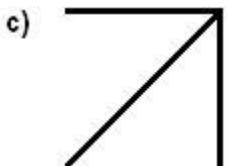
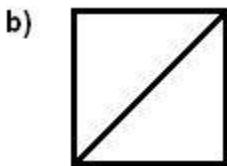
b) K_{4,4}

c) K_{3,4}

d) K_{3,5}



9) Draw the dual graph of this map.



10) Convert the incidence matrix

$$\begin{bmatrix} 1 & 1 & 1 & 0 & 0 & 0 \\ 1 & 0 & 0 & 1 & 1 & 0 \\ 0 & 1 & 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 1 & 1 & 0 \end{bmatrix}$$

to adjacency matrix.

a)

$$\begin{bmatrix} 0 & 1 & 1 & 1 \\ 1 & 0 & 0 & 2 \\ 1 & 0 & 1 & 0 \\ 1 & 2 & 0 & 0 \end{bmatrix}$$

b)

$$\begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 0 & 1 & 1 \\ 1 & 1 & 0 & 2 \\ 0 & 1 & 2 & 0 \end{bmatrix}$$

c)

$$\begin{bmatrix} 1 & 0 & 1 & 1 \\ 0 & 0 & 0 & 2 \\ 1 & 0 & 0 & 1 \\ 1 & 2 & 1 & 0 \end{bmatrix}$$

d)

$$\begin{bmatrix} 0 & 0 & 2 & 0 \\ 0 & 0 & 1 & 1 \\ 2 & 1 & 1 & 1 \\ 0 & 1 & 1 & 0 \end{bmatrix}$$

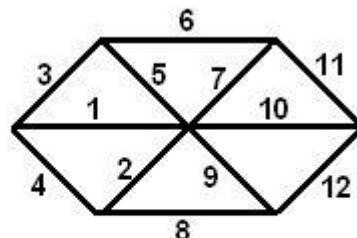
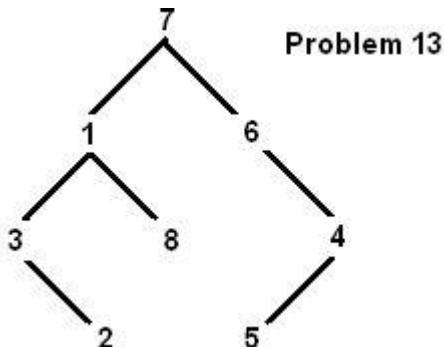
PART (II) Each problem is worth 5 points. Write complete solutions.

11) Evaluate GCD(2007,522) using Euclidean Algorithm.

12) Find the matrix of the transitive closure of the relation given by

$$\begin{bmatrix} 0 & 0 & 1 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

13) Write the output using (a) pre-order (b) post-order (c) in-order algorithms.



Problem 14

14) Draw the minimal spanning tree and find its value.

-Amin Witno