



**PHILADELPHIA UNIVERSITY**  
**DEPARTMENT OF BASIC SCIENCES**

**Final Exam A**

**DISCRETE STRUCTURES**

**04-02-2014**

**PART (I)** Each problem is worth 2 points. Circle one answer.

1) Evaluate LCM (493, 323).

- a) 7429      b) 8303      c) 8381      d) 9367

2) How many permutations with { A, B, C, D, E, F } do not contain "ACE" ?

- a) 24      b) 120      c) 696      d) 714

3) Let  $A = \{2, 5, 6, 7, 9\}$  and the equivalence relation  $R = \{(a,b) \mid a \bmod 2 = b \bmod 2\}$ . Find the equivalence classes.

- a)  $\{2, 6\}, \{5, 7, 9\}$       b)  $\{2, 7, 9\}, \{5, 6\}$   
c)  $\{2, 4, 8\}, \{5, 7\}$       d)  $\{2, 7, 8\}, \{4, 5\}$

4) Let  $R = \{(1,3), (2,1), (3,2), (4,2)\}$ . Then  $R^3 =$

- a)  $\{(1,2), (2,3), (3,1), (4,1)\}$       b)  $\{(1,1), (2,2), (3,3), (4,3)\}$   
c)  $\{(1,4), (2,3), (3,1), (4,3)\}$       d)  $\{(1,1), (2,4), (3,3), (4,4)\}$

5) How many integers from 1 to 1000 are multiples of 4 and not of 6 ?

- a) 63      b) 84      c) 126      d) 167

6) Which graph has 12 edges?

- a)  $P_6$       b)  $C_6$       c)  $K_6$       d)  $K_{2,6}$

7) Which graph has the largest diameter?

- a)  $C_9$       b)  $K_9$       c)  $P_9$       d)  $K_{9,9}$

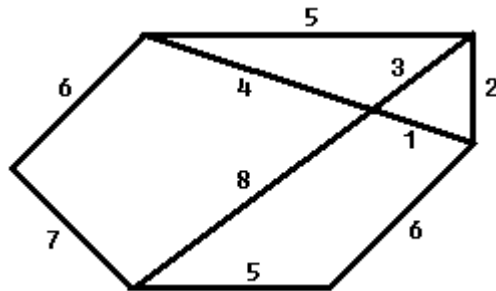
8) Which graph has an Euler circuit?

- a)  $K_6$       b)  $K_9$       c)  $K_{2,9}$       d)  $K_{1,6}$

9) Convert the incidence matrix  $\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 \\ 1 & 1 & 0 & 1 \\ 0 & 0 & 1 & 1 \end{bmatrix}$  to adjacency matrix.

- a)  $\begin{bmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 1 & 1 \\ 1 & 1 & 0 & 1 \\ 0 & 1 & 1 & 0 \end{bmatrix}$     b)  $\begin{bmatrix} 0 & 0 & 1 & 1 \\ 0 & 0 & 1 & 1 \\ 1 & 1 & 0 & 0 \\ 1 & 1 & 0 & 0 \end{bmatrix}$     c)  $\begin{bmatrix} 0 & 1 & 1 & 0 \\ 1 & 0 & 1 & 1 \\ 1 & 1 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}$     d)  $\begin{bmatrix} 0 & 1 & 1 & 0 \\ 1 & 0 & 0 & 1 \\ 1 & 0 & 0 & 1 \\ 0 & 1 & 1 & 0 \end{bmatrix}$

10) Find the weight of the minimal spanning tree (MST) for the given graph.



- a) 21    b) 23    c) 24    d) 28

**PART (II)** Each problem is worth 5 points. Write complete solutions.

11) Convert the proposition  $(P \leftrightarrow Q) \rightarrow R$  to CNF.

12) Use induction to prove  $2^n < n!$  for all integer  $n \geq 4$ .

13) Let  $A = \{ 2, 3, 6, 9, 18 \}$  and  $R = \{ (a,b) \mid b \bmod a = 0 \}$ .

- a) Draw the graph of R.  
 b) Prove that R is a partial order relation.  
 c) Draw the Hasse diagram for R.

14) Solve the Chinese postman problem (CPP) for the given graph.

