

PHILADELPHIA UNIVERSITY  
DEPARTMENT OF BASIC SCIENCES

**Exam 1**

**Number Theory**

**05–11–2012**

Solutions must be complete in order to receive full credit.

1. Is the number 299 prime or composite? Use trial division.
2. Evaluate  $\gcd(18900, 105840)$  by factoring into primes.
3. Evaluate  $\gcd(54321, 12345)$  using the Euclidean algorithm.
4. Find all the integer solutions of  $28x + 49y = 35$ .
5. Prove that  $60 \mid n^5 - 5n^3 + 4n$  for any integer  $n$ .

–Amin Witno

The list of primes below 200.

2	3	5	7	11	13	17	19	23	29
31	37	41	43	47	53	59	61	67	71
73	79	83	89	97	101	103	107	109	113
127	131	137	139	149	151	157	163	167	173
179	181	191	193	197	199				