

PHILADELPHIA UNIVERSITY  
DEPARTMENT OF BASIC SCIENCES

Exam 1

Computational Number Theory

24-03-2009

1. Given that  $1187^2 \equiv 632^2 \pmod{3959}$ . Factor the number 3959 by computing GCD using the Euclidean algorithm.
2. In RSA, Alia selects  $n = 319$  and  $e = 19$ . If the intended message is  $m = 66$ , compute  $s = m^e \% n$  using successive squaring algorithm.
3. In RSA, suppose that  $n = 11371$  and it is known that  $\phi(n) = 11152$ . Factor  $n$  using the quadratic formula.
4. Illustrate Fermat factorization using the number  $n = 12533$
5. Write  $n = 10t + u$ . Prove that  $19 \mid n$  if and only if  $19 \mid t + 2u$ .

-Amin Witno